

WARM UP:

p. 476 #3, 5

p-value = the probability of getting our sample (or something more extreme) if the claim is still true.

p. 476 #3, 5

3) Letter (D) is the only correct response. It is the definition of a p-value.

$$\begin{aligned} H_0: p &= 0.30 \\ H_a: p &< 0.30 \end{aligned}$$

5) $H_0: p = 70\%$
 $H_a: p > 70\%$

p-value = 0.27

The p-value is very large, so we fail to reject the H_0 and say that we think the percent is equal to 70%. Therefore the new medication did not increase relief. It is equally effective as the old med.

HW: p. 476 #4, 10, 17, 19

HOMEWORK:

4) $H_0: p = 1/6$ ** $p =$ percent of 6's
 $H_a: p > 1/6$

$p\text{-value} = 0.03$

letter (d) is the correct conclusion.

10) $H_0: p = 0.90$ -1

$H_a: p \neq 0.90$ -1

Conditions:

SRS, $750 > 10$ -2.5

$np > 10$
 $nq > 10$

pop > 10n

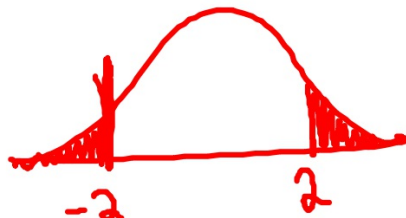
Statement

-2

$\hat{p} = 657/750 = 0.876$; $SD(p) = \sqrt{\frac{(0.90)(0.10)}{750}} = 0.012$
-1/2

$Z = \frac{0.876 - 0.90}{0.012} = -2$ -1

$P(Z < -2) = 0.977$ -1



-4

There is more than a 97% chance that the stated percentage is correct for this region.

17) (a) $H_0: p = 0.63$
 $H_a: p > 0.63$

$p = 0.63$
 $n = 240$
 $\hat{p} = 163/240 = 0.679$

(b) STATE:

- SRS
- $np \geq 10$
- $nq \geq 10$
- $pop \geq 10n$

CHECK:

stated representative

$$(240)(0.63) \geq 10$$

$$(240)(0.37) \geq 10$$

there are more than 2400 students
that use LSATisfaction training

Conditions met --> Normal Model --> 1 prop Z test

$$Z = \frac{0.6792 - 0.63}{\sqrt{\frac{(0.63)(37)}{240}}} = 1.571$$

$$P(Z > 1.571) = \text{normcdf}(1.571, \text{E99}, 0, 1) = 0.0581$$

We fail to reject H_0 because p-value of 0.0581 is greater than $\alpha = 0.05$. We have insufficient evidence that the true % of law school applicants who were admitted after taking the training program is greater than 63%.

(c) No. There is no evidence that the program increased the % of people who were admitted to law school.

19) (a) $H_0: p = 0.20$
 $H_a: p > 0.20$

$$p = 0.20$$

$$n = 22$$

$$\hat{p} = 7/22 = 0.318$$

pop = 150

(b) STATE:

- SRS
- $np \geq 10$
- $nq \geq 10$
- $\text{pop} \geq 10n$

CHECK:

will have to assume representative

$$(22)(0.20) \geq 10$$

$$(22)(0.80) \geq 10$$

there are NOT more than 220 cars in the fleet

We can NOT use our Normal Model for our 1-Prop Z-test

If you proceeded anyway...

$$z = \frac{\hat{p} - p}{\sqrt{\frac{p \cdot q}{n}}} = 1.383$$

$$P(Z > 1.383) = \text{normcdf}(1.383, \text{E99}, 0, 1) = 0.0833$$

We fail to reject H_0 b/c P-value of 0.0833 is greater than our alpha of 0.05. We have insufficient evidence that the true % of cars that fail emissions testing is greater than 20%.

CH. 20 PRACTICE

BOOK PROBLEMS:

p. 477

#12- add letter (g) create an appropriate conf. interval

#14- add letter (f) create an appropriate conf. interval

#20 (why can't you do this one?)

12) (a) $H_0: p = 0.05$
 $H_a: p > 0.05$

$$p = 0.05$$

$$n = 384$$

$$\hat{p} = 46/384 = 0.1198$$

(b) Conditions:

- SRS assumed representative
- $np \geq 10$ $19.2 \geq 10$
- $nq \geq 10$ $364.8 \geq 10$
- $\text{pop} \geq 10n$ there are more than 3840 children

Conditions met --> $N(0.05, 0.01112)$ --> 1-Prop Z-test

12) (c)

$$z = \frac{0.1198 - 0.05}{\sqrt{\frac{(0.05)(0.95)}{384}}} = 6.275$$

$$P(Z > 6.275) = 1.754 \times 10^{-10}$$

(d) The probability of getting a sample where 11.98% or more of the children show abnormalities is 1.754×10^{-10} , if the true % of abnormalities has not changed from 5%.

12)

- (e) We reject H_0 b/c P-value of 1.754×10^{-10} is $< \alpha = 0.05$.
We have sufficient evidence that the true percent of children with abnormalities is above 5%.

- (f) We cannot say there is a cause and effect relationship.
We can only say that our sample gives us strong evidence that the % of abnormalities has increased from 5%.

(g) Confidence interval: 90%

conditions met --> $N(0.1198, 0.0166)$ --> 1 prop Z Interval

$$0.1198 \pm (1.645)(0.0166) = (0.09254, 0.14705)$$

We are 90% confident that the true percent of children with abnormalities is between 9.254% and 14.705%.

14) (a) $H_0: p = 0.31$
 $H_a: p \neq 0.31$

$p = 0.31$
 $n = 8368$
 $\hat{p} = 0.32$

(b) Conditions:

- SRS assumed representative
- $np \geq 10$ $(8368)(0.31) \geq 10$
- $nq \geq 10$ $(8368)(0.31) \geq 10$
- $pop \geq 10n$ there are more than 83680 students

Conditions met --> $N(0.31, 0.0051)$ --> 1-Prop Z-test

14) (c)

$$Z = \frac{0.32 - 0.31}{\sqrt{\frac{(0.31)(0.69)}{8368}}} = 1.9836$$

$$2 * P(Z > 1.9836) = 0.0473$$

(d) We reject H_0 b/c P-value of 0.0473 is less than our alpha of 0.05. We have sufficient evidence that the true % of mothers who have graduated from college is not 31% anymore.

(e) No. The P-value is only slightly below alpha.

(f) confidence level: 95%

conditions met --> $N(0.32, 0.0051)$ --> 1 prop Z Interval

$$0.32 \pm (1.96)(0.0051) = (0.31003, 0.33002)$$

We are 95% confident that the true percent of mothers who have graduated from college is between 31.003% and 33.002%.

20) the np and $nq \geq 10$ condition is not satisfied,
therefore we cannot proceed with the test

We would need a larger sample size if we wanted
to proceed

Full credit on tests...

- * Get out a blank piece of paper
- * Close your notes
- * Get out your formula sheet
- * Complete #27 in book
 - on your own, silently
 - no help from me or classmates

27) (a) $H_0: p = 0.103$
 $H_a: p > 0.103$

2

$p = 0.103$
 $n = 1782$
 $\hat{p} = 0.1178$

(b) Conditions:

- SRS

assumed representative

3

- $np \geq 10$

$(1782)(0.103) \geq 10$

$nq \geq 10$

$(1782)(0.897) \geq 10$

- $\text{pop} \geq 10n$

there are more than 17820 high school students

Conditions met, Normal Model, 1-Prop Z-test

2

$$Z = \frac{0.1178 - 0.103}{\sqrt{\frac{(0.103)(0.897)}{1782}}} = 2.0616$$

$$P(Z > 2.0616) = 0.0196$$

We reject H_0 b/c P-value of 0.0196 is less than our alpha of 0.05. We have sufficient evidence that the true % of high school dropouts is greater than 10.3%. There is evidence that the dropout rate is increasing.